Matching large ontologies: A divide-and-conquer approach

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ARTICLE INFO
Article history:
Received 28 January 2008
Received in revised form 9 June 2008
Accepted 11 June 2008
Available online 20 June 2008

Keywords:
Ontology matching
Data integration
Semantic heterogeneity

ABSTRACT
Ontologies proliferate with the progress of the Semantic Web. Ontology matching is an important way of establishing interoperability between (Semantic) Web applications that use different but related ontologies. Due to their sizes and monolithic nature, large ontologies regarding real world domains bring a new challenge to the state of the art ontology matching technology. In this paper, we propose a divide-and-conquer approach to matching large ontologies. We develop a structure-based partitioning algorithm, which partitions entities of each ontology into a set of small clusters and constructs blocks by assigning RDF Sentences to those clusters. Then, the blocks from different ontologies are matched based on precalculated anchors, and the block mappings holding high similarities are selected. Finally, two powerful matchers, V-DOC and GMO, are employed to discover alignments in the block mappings. Comprehensive evaluation on both synthetic and real world data sets demonstrates that our approach both solves the scalability problem and achieves good precision and recall with significant reduction of execution time.

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1. Introduction

The Semantic Web is an effort by the W3C Semantic Web Activity to achieve data integration and sharing across different applications and organizations. Ontologies, as a new representational form of knowledge, play a prominent role in the development and deployment of the Semantic Web. To date, the popularity of ontologies is rapidly growing, and the amount of available ontologies continues increasing. For example, an ontology search engine, SWOOGLE [12], reports that it has collected more than 10,000 ontologies on the Web so far.

Due to the decentralized nature of the Web, there usually exist multiple ontologies from overlapped application domains or even within the same domain. In order to establish interoperability between (Semantic) Web applications that use different but related ontologies, ontology matching has been proposed as an effective way of handling the semantic heterogeneity problem. It is typically useful to some data management applications, such as information integration and distributed query processing.

Generally, the well-known “80/20” rule applies in ontology matching [1]. Automatic matching algorithms and tools can automate 80% of the work, covering common cases and creating results that are close to correct. As surveyed in [16], a wide range of characteristics in ontologies to be matched are exploited by existing approaches, such as linguistic descriptions (e.g., rdfs:label), structural information (e.g., rdfs:subClassOf) and data instances. In addition, some of them also utilize background knowledge from thesauri or third parties’ ontologies. The rest 20% requires manual contribution to perfect portions of the results. Past work mainly focuses on human collaboration [40,65] and matching visualization [1,9,17,36], which significantly facilitate matching understanding and refinement. In this paper, we aim at proposing automatic approaches for ontology matching.
Based on our investigation, most of the state of the art automatic approaches are merely applicable for small-scale ontologies, and the effectiveness of these approaches decreases for large ontologies. As concluded in the latest Ontology Alignment Evaluation Initiative 2007 (OAEI) [15], 17 ontology matching tools joined the campaign, but only four tools (including the one described in this paper) accomplished all the three matching tasks with large ontologies (Anatomy, Food and Library). But, the other three tools, namely DSSIM [43], RIMOM [58] and PRIOR+ [39], do not really solve the large ontology matching problem. DSSIM manually partitions large ontologies into several smaller pieces, while RIMOM and PRIOR+ use simple string comparison techniques as alternatives.

As of today, there are quite a lot of applications that require matching large ontologies. For example, in library management, large book classification categories, such as Brinkman and GTT thesauri,¹ are needed to be integrated to remove redundant books. For another example, in the medicine and biology domains, large life-science ontologies, e.g., GALEON² and FMA [50], are required to be matched in order to provide a uniform service for access and manipulation [63]. Therefore, these emerging demands on matching large ontologies bring a new challenge to the state of the art ontology matching technology.

It is our goal in this paper to explore ways of matching large ontologies. The main principle of our approach is based on the divide-and-conquer philosophy. The framework of the approach is illustrated in Fig. 1. Specifically, the input is two large ontologies to be matched. The approach firstly partitions the entities (i.e., classes and properties) of each ontology into a set of small clusters by measuring their structural proximities, and then constructs blocks via assigning RDF Sentences [64] (i.e., a kind of integrated units over RDF triples) to the clusters (Phase 1). Those blocks are matched based on precalculated anchors (i.e., matched entities gained beforehand), and block mappings (i.e., matched blocks with high similarities) are selected (Phase 2) to be further matched by two powerful matchers, V-Doc [46] and GMO [27], for outputting alignments (Phase 3). In this paper, we focus on the ontologies written in RDFS [5] or OWL [45], because they are the latest common formats recommended by W3C for publishing ontologies. Furthermore, the work in [8] has analyzed 3959 ontologies available on the Web, in which 3258 (nearly 82%) are expressed in RDFS or OWL.

Our approach has two major advantages. Firstly, it solves the scalability problem of matching large ontologies, i.e., it does not suffer from lack of memory (e.g., the “out of memory” error, which is caused by not enough memory to be allocated). According to the OAEI 2007 report, most matching tools can only work on small ontologies with hundreds of entities, while our approach can deal with very large ontologies with ten thousands of entities. Secondly, it significantly decreases the execution time with pretty good quality. For example, two large ontologies are provided in the Anatomy track of OAEI 2007 [15], each one contains about 3000 entities. DSSIM, RIMOM and PRIOR+ spend 75 min, 4 h and 23 min to complete the task, respectively, while our approach merely takes 12 min. More importantly, as compared to DSSIM, RIMOM and PRIOR+, our approach achieves better (or at least comparable) precision and recall.

It is also worthy of noting that the approach presented in this paper substantially improves our previous conference paper [30] with the following aspects: (1) it utilizes RDF Sentences [64] as basic units to construct blocks from the clusters. RDF Sentences provide more integrated syntactic and semantic structures than RDF triples (i.e., statements), since they encapsulate blank nodes. As a result, the completeness of blank nodes, which is the lowest requirement for blocks, is preserved; (2) it extends the partitioning algorithm for properties in ontologies, while our previous work only copes with class hierarchies; (3) it integrates two powerful matchers, V-Doc and GMO, to discover alignments; and (4) we comprehensively evaluate our approach on both synthetic and real world data sets. In the synthetic test, two new kinds of metrics (the partitioning quality

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¹ http://stitch.cs.vu.nl/ – semantic interoperability to access cultural heritage.
² http://www.opengalen.org/
and the mapping quality) are defined to assess the effectiveness of our approach. In the real world test, we attended OAEI 2007 and compared our approach with other participants.

The remainder of this paper is organized as follows: Section 2 defines the terminologies and notations used in this paper. Section 3 discusses related work. Section 4 presents the computation of structural proximities, the partitioning algorithm and the construction of blocks. Section 5 introduces the approaches to anchor generation and block matching. Section 6 summarizes two matchers V-DOC, GM0 and our combination strategy. Section 7 reports experimental results on both synthetic and real world data sets. Finally, Section 8 concludes the paper with future work.

2. Problem formulation

An ontology is a formal, explicit specification of a shared conceptualization [21]. In this paper, we use a basic definition of ontologies based on the RDF graph model [35,45], which is general enough to cover most of the state of the art large ontologies.

Definition 1. (ontology) An ontology $\mathcal{O}$ is a set of RDF triples $T$. Any RDF triple $t$ ($t \in T$) denotes a statement of the form (subject, predicate, object). Any node in an RDF triple may be a URI with an optional local name (URIref), a literal, or a blank node (having no separate form of identification). A predicate is always a URIref, and a literal cannot be a subject.

Without explanation, ontologies shown in this paper are expressed in RDFS or OWL. An OWL ontology can easily be transformed to an RDF graph [45]. In our notation, we use $c$ to represent a class and $p$ to represent a property. The specification [5] provides the basic mechanism to recognize classes and properties from nodes in RDF triples. For simplicity, classes and properties are uniformly called entities ($d$ denotes an entity). In this paper, we consider an ontology containing more than one thousand entities as a large ontology.

Ontology matching (also called mapping or aligning) aims at discovering alignments (also named mappings, correspondences or matches) between semantically similar entities in different ontologies. These alignments might stand for equivalence as well as other relationships, such as subsumption or disjointness, between entities [16]. Alignments can be used in a variety of applications, such as ontology merging, query answering, data translation or for browsing the Semantic Web. Inspired by the definitions in [54], we define ontology matching as follows.

Definition 2. (ontology matching) Let $\mathcal{O}_0, \mathcal{O}_1$ be two ontologies. Matching $\mathcal{O}_0$ with $\mathcal{O}_1$ finds a set of alignments $A = \{a_1, a_2, \ldots, a_n\}$. Each $a_i$ ($i = 1, 2, \ldots, n$) is a 5-tuple: $(id_1, d, d', u, v)$, where $id_1$ is a unique identifier; $d$ is an entity in $\mathcal{O}_0$, and $d'$ is an entity in $\mathcal{O}_1$; $u$ is an equivalence ($\equiv$), subsumption ($\subseteq$ or $\supseteq$) or disjointness ($\perp$) relationship holding between $d$ and $d'$; and $v$ is a similarity between $d$ and $d'$ in the $[0, 1]$ range.

In this paper, matching large ontologies specifically indicates each of the ontologies to be matched is large, rather than matching a large amount of small ontologies (called holistic matching in [25]). Furthermore, we only consider the equivalence relationship between entities.

Precisely defining blocks requires the notion of the RDF Sentence, so we first give the definition of the RDF Sentence [64]. An equivalent definition of the RDF Sentence is the minimum self-contained graph [60]. Following the theorems in [60], an RDF graph can be decomposed into a unique set of RDF Sentences.

In RDF (also RDFS and OWL), there is a special kind of nodes, called blank nodes (or bnodes), which are not identified by URLs. Blank nodes are a sort of existentially quantified resource whose meaning is in the scope of the triples it appears. RDF triples sharing a common blank node provide an integrated structure indicating a joint context of the blank node, and if such triples are separated, the context is broken. For example, in the left part of Fig. 2, the ontology $\mathcal{O}$ has a blank node _:genid, which is shared by three RDF triples: $t_1$, $t_2$, $t_3$. Those three triples form a restriction structure, which constrains a Reference at least has One Author. At present, RDF semantics [35] does not provide any intrinsic mechanism to guarantee this kind of structure. We define it as an RDF Sentence.

We say that two RDF triples are b-connected if they share blank nodes. An RDF Sentence is the maximum closure of the b-connected RDF triples.$^3$

Definition 3. (RDF Sentence) Let $\mathcal{O}$ be an ontology. An RDF Sentence $s$ is a set of RDF triples, which satisfies the following conditions:

1. $s \subseteq \mathcal{O}$;
2. $\forall t_i, t_j \in s, i \neq j, t_i, t_j$ are b-connected;
3. $\forall t_i \in s, t_i \notin s, t_i, t_j$ are not b-connected.

$^3$ In implementation, ontology parsing tools usually assign system-generated internal names to blank nodes. We transform an RDF graph into an undirected triple graph, where each vertex represents an RDF triple in the original RDF graph. An edge exists between two RDF triples iff they contain blank nodes having the same name. We call that the two RDF triples share a blank node. Then, each connected component in the triple graph forms an RDF Sentence.
An RDF triple whose subject is not a blank node is defined as a main RDF triple. In principle, an RDF Sentence is composed of a main RDF triple, and all the other triples in the RDF Sentence are b-connected to it. The subject of an RDF Sentence is the subject of its main RDF triple.

Now, we give the definition of blocks by using RDF Sentences as basic units instead of RDF triples.

Generally speaking, a block can be viewed as a subset of an ontology (i.e., a set of triples). Compared to a module [20] or a cluster [22], a block is neither strictly complete in logics nor merely a complete set of entities. For example, in [20], an ideal module guarantees to capture the meanings of the entities in an OWL DL ontology. That is, when answering arbitrary queries against an ontology, importing the module would give us exactly the same answers as if we had imported the whole ontology. A cluster is comprised of a set of similar entities grouped together. A partitioning breaks all the entities in an ontology into a set of clusters, satisfying: (1) for any two different clusters, they are disjoint; and (2) the union of all the clusters equals the entire set of the entities.

**Definition 4.** (block) Let \( \mathcal{O} \) be an ontology and \( D \) be a set of all the entities in \( \mathcal{O} \). A partitioning, \( G \), of \( D \) breaks \( D \) into a set of clusters \( \{g_1, g_2, \ldots, g_n\} \), which satisfies: (1) \( \bigcap_{i=1}^{n} g_i = \emptyset \) and \( i \neq j, g_i \cap g_j = \emptyset \); and (2) \( g_1 \cup g_2 \cup \cdots \cup g_n = D \). Let \( b_i \) be the block corresponding to a cluster \( g_i \) (\( i = 1, 2, \ldots, n \)). A block is a union of RDF Sentences \( (b_i = \{b_1, b_2, \ldots, b_m\}) \), where each \( b_i \) (\( k = 1, 2, \ldots, m \)) satisfies subject \( (s_k) \in g_i \), \( \forall b_i, b_j, i, j = 1, 2, \ldots, n \) and \( i \neq j, b_i \cap b_j = \emptyset \).

In this paper, we carefully differentiate between clusters and blocks. A cluster is a set of entities, while a block is a set of RDF triples. For any two different blocks, the triples in the two blocks are disjoint. But, the entities contained in these triples may overlap. Furthermore, the union of all the blocks occasionally does not equal to the entire ontology, because a kind of RDF triples is missing: those triples with blank nodes as subjects that have never been objects (e.g., owl:AllDifferent).

A block mapping is a pair of matched blocks from two ontologies. We refer to the process of discovering block mappings as block matching. In this paper, please note that we allow a block to appear in several block mappings and do not specify the relationship of two blocks within a block mapping.

**Definition 5.** (block matching) Let \( B, B' \) be two sets of blocks derived from two ontologies \( \mathcal{O}, \mathcal{O}' \), respectively. Block matching \( B \) with \( B' \) finds a set of block mappings \( BM = \{b_1, b_2, \ldots, b_m\} \). Each \( b_m \), \( i = 1, 2, \ldots, n \) is a 4-tuple: \( (id_2, b, b', f) \), where \( id_2 \) is a unique identifier; \( b, b' \) are two blocks in \( B, B' \) respectively; and \( f \) is a similarity between \( b \) and \( b' \) in the [0, 1] range.

To help understand, we illustrate a toy example here. Let us see the two ontologies shown in Fig. 2 (typing triples are not depicted in the figure). The ontology \( \mathcal{O} \) in the left part includes six classes Reference, Book, Inproceedings, Monograph, Person and Author; and one property hasAuthor. We can generate three blocks \( b_1, b_2, b_3 \) (enclosed by dotted lines) from three clusters \( g_1 = \{\text{Reference}, \text{Book}, \text{Inproceedings}, \text{Monograph}\}, g_2 = \{\text{Author}, \text{Person}\}, g_3 = \{\text{hasAuthor}\} \). Note that the triples among \( b_1, b_2 \) and \( b_3 \) are disjoint, not the entities. For example, hasAuthor is shared by \( b_1 \) and \( b_3 \), but the RDF triple \( t_0 \) only belongs to \( b_3 \). The ontology \( \mathcal{O}' \) in the right part has five entities: Entry, Book, ConferencePaper, Author, and hasAuthor.
3. Related work

Although quite a lot of work has addressed the ontology matching problem, there are few generic approaches that raise the issue of matching large ontologies. In this section, we will focus on discussing related work on large ontology matching. Regarding matching small ontologies, it has been well surveyed in literature, and we refer the reader to [14,16,31,44,48,54].

3.1. Large ontology matching

To match large ontologies, a few light-weight ontology matching approaches, on the one hand, can be directly used. For example, edit-distance based methods [37,55] compute the similarity between two strings (e.g., rdfs:label(s)) by counting the number of operations required to transform one of them into the other. Because they only compare two strings in each time, they do not have the scalability limit and can be applied to match ontologies with any size. On the other hand, some work adapts the matching algorithms to reduce memory consumption. For example, the work in [42] simplifies a graph matching algorithm to match two large medical taxonomies by only considering the direct children and grandchildren of entities. Besides, using proper data structures (e.g., sparse matrices) and secondary storage (e.g., hard disks) might also facilitate large ontology matching. Compared with these methods, our approach addresses the problem from another direction based on the divide-and-conquer strategy.

In addition, there exist some domain-specific approaches that address matching large ontologies in particular areas (e.g., in biology [34,63] and geography [9]). Usually, they utilize certain light-weight methods to gain initial candidates and use domain knowledge to infer alignments. AOAS [63] is a representative tool that is heavily specialized on matching biomedical ontologies and makes extensive use of medical background knowledge. For the Anatomy track in OAEI 2007, it takes a broader ontology PLEA as the background knowledge to further improve the initial results. Because these approaches heavily depend on domain knowledge, they are not general-purpose solutions and easily fail when such knowledge is unavailable. But, if there is proper background knowledge, they can find some complex and interesting alignments.

In OAEI 2007, three generic ontology matching tools, DSSIM [43], RIMOM [58] and PRIOR+ [39], took part in all the three tracks with large ontologies. DSSIM designs a query-like framework, which expands each entity from one of the two ontologies to be matched to a query fragment in terms of WordNet. RIMOM is based on the risk minimization model and integrates seven different ontology matching strategies, each one aims at a specific ontological information. PRIOR+ is an automatic ontology mapping tool based on propagation theory, information retrieval technique and artificial intelligence model. Although the three tools showed their results for the large ontology matching tracks, they do not propose methods to solve the problem. DSSIM manually divides large ontologies into small blocks, while RIMOM and PRIOR+ adopt edit-distance based methods as alternatives.

3.2. Ontology partitioning

In the first stage of our approach, two ontologies are partitioned into two sets of blocks, so it may be broken down into the category of ontology modularization. Among the literature, some representative work is in [20,52,56]. The work in [52] introduces a way of constructing stand alone fragments by exhaustively traversing various links (i.e., properties) from a specified entity. The work in [56] presents a framework based on Distributed Description Logics, which uses bridge rules to support modularization. But, the mechanism for manipulating the sizes of the modules is not clear. The work in [20] studies the problem of extracting minimal modules by approximation in the context of collaborative ontology development and controlled integration, which makes the sizes of the modules relatively small. These ontology modularization approaches have realized the importance of scalability and made progress in reducing the sizes of modules, however, they still have the scalability problem and are inapplicable in the context of matching large ontologies yet. For example, by applying the approach in [20] to GALLEN, the maximum module still owns more than 7000 entities, which is not an easily manageable scale for the state of the art matching approaches. Our partitioning approach aims at controlling the sizes of blocks, while it still satisfies the lowest requirement for modules, i.e., the completeness of blank nodes in blocks [60]. However, please note that, if such modularization approaches could flexibly control the sizes of modules in the future, they might be used to replace our partitioning approach.

Although the major contribution of the work in [59] is ontology visualization, it also gives a way of partitioning large ontologies by using a data clustering algorithm (the Force Directed Placement algorithm). The basic ideas of the approach in [59] and our approach are the same, and both of them transform ontologies into graphs and use clustering algorithms to partition the graphs. However, compared to it, not only does our approach partition entities in an ontology to disjoint clusters hierarchically, but it also uses RDF Sentences to recover RDF triples to the clusters, while the method in [59] does not provide any mechanism to preserve the triples that contain blank nodes.

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4 http://wordnet.princeton.edu/.
3.3. Block matching

To the best of our knowledge, BMO [28] and COMA [2,13,49] are the only two work we know so far that consider the block matching problem. BMO matches two ontologies from a linguistic perspective and generates a similarity matrix. Afterwards, it applies a spectral partitioning algorithm to that similarity matrix to obtain block mappings directly. Because it requires to match two full ontologies, it may suffer from the scalability problem and be not feasible to match large ontologies. Besides, it uses a linguistic measure to calculate the distances between entities, so the quality of its generated blocks is not good.

COMA is a generic schema and ontology matching tool, providing a collection of elementary matchers and a flexible infrastructure to combine those matchers. It develops a fragment-based matching method to solve the large schema matching problem. It transforms each ontology into a directed acyclic graph and decomposes the graph from top to bottom. During decomposition, when the number of entities in any block exceeds a pre-defined value, a compaction function would be called to the bottom entities in the block. As a result, the descendants of a bottom entity are all represented by the entity, and another block starts construction. It is originally used to partition database schemas or XML schemas, which are usually represented as trees rather than complex graphs, so it does not well fit ontologies that have complex structures. Another problem is that it ignores the different features of classes and properties. So, the partitioning quality of COMA is not very good. Besides, when matching fragments, it merely uses the local descriptions of roots to represent the whole fragments, therefore some matched fragments may be skipped.

In schema matching (see [14,48]), IMe [10] semi-automatically finds both 1:1 and very complex alignments (e.g., room – price = room – rate · (1 + tax – rate)). It embeds two kinds of domain knowledge (overlapped data and external data) to infer complex alignments. However, it is hard to specify the domain knowledge in some cases, and the granularity of those complex alignments is low. Artemis [6] is another work that vaguely presents the idea of block matching. It computes the 1:1 alignments between two schemas by using WordNet and generates block mappings from the 1:1 alignments via a clustering algorithm. This is similar to the framework of BMO. Hence, it also suffers from the high computational complexity for finding the 1:1 alignments.

4. Partitioning ontologies

In this section, we will first present the measure of structural proximities (see Phase 1.1 in Fig. 1). Then, we will introduce an agglomerative algorithm to partition entities into a number of clusters based on the structural proximities (Phase 1.2). Finally, we will describe the construction of blocks by assigning RDF Sentences to the clusters (Phase 1.3).

4.1. Computing structural proximities

According to the investigation in [3], a large number of ontology design patterns are employed during the development of ontologies. For large ontology construction, we highlight two design principles. The first principle is named the classification principle, which categorizes and specifies concepts (e.g., in FMA [50]) so that the taxonomy feature is depicted; the second one is the modularization principle [56], which provides different levels of granularity to support maintenance and re-use. These two kinds of principles are mainly revealed in the hierarchies of large ontologies, i.e., embedded in the rdfs:subClassOf and rdfs:subPropertyOf relationships between entities. They inspire us to measure the hierarchical distances in order to characterize their structural proximities.

Structural proximities between classes are defined based on how closely they are related in the hierarchies of the rdfs:subClassOf relationships. Let $c_i$, $c_j$ be two classes in a given ontology $\mathcal{C}$, the structural proximity between $c_i$ and $c_j$ is:

$$\text{prox}(c_i, c_j) = \frac{2 \cdot \text{depth}(c_i) \cdot \text{depth}(c_j)}{\text{depth}(c_i) + \text{depth}(c_j)},$$  \hspace{1cm} (1)

where $c_i$ is the common superclass of $c_i$ and $c_j$, and depth($c_i$) gets the depth of $c_i$ in the original class hierarchy (i.e., without inferencing). Please note that these class hierarchies of large ontologies are usually represented as directed acyclic graphs (if there exists any cycle, we break up the cycle by arbitrarily removing an edge) rather than trees, so the depth of $c_i$ is not unique. In this paper, we choose the maximum one as the depth of $c_i$, since it is most specific in semantics. Also, the common superclass of $c_i$ and $c_j$ is not unique, so we choose the one, which has the maximum depth, as the common superclass of $c_i$ and $c_j$.

Formula (1) gives two meanings: (1) the deeper the common superclass of two classes is, the closer the two classes are; and (2) the structural proximity of two classes strengthens as their depths increase. For example, let us consider five classes: Object, Human, Animal, Woman and Man. Woman and Man are two subclasses of Human, while Human and Animal are two subclasses of Object. Hence, Woman and Man are closer than Human and Animal. (If we assume that the depth of Object is 1, then $\text{prox}(\text{Man, Woman}) = 2 \cdot 2 / (3 + 3) > 2 \cdot 1 / (2 + 2) = \text{prox}(\text{Human, Animal})$.)

Formula (1) has also been presented in [59] for ontology browsing. In practice, for many popular ontology visualization tools such as Protégé,\(^5\) class hierarchies are the most important structure for browsing. Also, in large ontologies, the number

\(^5\) http://protege.stanford.edu/.
of the \textit{rdfs:subClassOf} relationships is considerably dominant as compared to others. For instance, \textsc{galen} contains nearly 10,000 classes and 30,000 RDF triples excluding typing triples and annotations, in which more than 18,000 triples are about \textit{rdfs:subClassOf}. Moreover, for thesauri such as \textsc{brinkman}, they only have the \textit{rdfs:subClassOf} relationships.

The hierarchies of the \textit{rdfs:subPropertyOf} relationships between properties are not so prevalent as the ones between classes. Therefore, structural proximities between properties are computed not only by how closely they are placed in the hierarchies but also by whether they have overlapped \textit{rdfs:domain(s)}. The properties with the overlapped \textit{rdfs:domain(s)} serve for the same class, so they are related. Let \(p_i, p_j\) be two properties in a given ontology \(\mathcal{O}\), the structural proximity between \(p_i\) and \(p_j\) is:

\[
\text{prox}(p_i, p_j) = \frac{\text{depth}(p_i)}{\text{depth}(p_i) + \text{depth}(p_j)} + \frac{|\text{dom}(p_i) \cap \text{dom}(p_j)|}{|\text{dom}(p_i)| + |\text{dom}(p_j)|},
\]

where \(\text{depth}(p_i)\) is the common super-property of \(p_i\) and \(p_j\), depth\(\text{depth}(p_i)\) gets the depth of \(p_i\) in the original property hierarchy, and \(\text{dom}(p_i)\) gets the domain\(\text{domains}\) of \(p_i\).

Besides, two optimizations are adopted: (1) some entities are identified as the same in a preprocessing stage, such as two entities are explicitly declared identical by using the \textit{owl:equivalentClass} or \textit{owl:equivalentProperty} relationships; and (2) only the structural proximities of entities having adjacent depths are measured in order to reduce the computational complexity, i.e., only computing the structural proximities of entities satisfying \(|\text{depth}(d_i) - \text{depth}(d_j)| \leq 1\). It is worthy of noting that this approximation is often used in structure-based partitioning approaches (e.g., in \cite{42}).

Let us see the example shown in Fig. 3. Given an ontology in the left part of the figure, after executing Phase 1.1, the structure proximities between the entities are depicted in the right part of the figure.

4.2. Partitioning

The objective of a partitioning algorithm is to partition a set of vertices \(V\) into a set of disjoint clusters \(g_1, g_2, \ldots, g_n\), where, by certain measure, the cohesiveness among the vertices in a cluster \(g_i\) is high; meanwhile the coupling crossing different clusters \(g_i, g_j\) is low. In the context of this paper, we seek to partition entities of an ontology into several clusters, so that the structural proximities among the entities in a cluster are high, while those crossing different clusters are low. Please note that the computed clusters satisfy the two conditions given in Section 2, i.e., any two different clusters are disjoint; and the union of all the clusters equals to the complete set of the entities.

The partitioning algorithm proposed in this paper is an agglomerative (i.e., bottom-up) partitioning algorithm mainly extended from \textsc{rock} \cite{22}, which is a very scalable agglomerative clustering algorithm in the area of data mining. The main difference between \textsc{rock} and our algorithm is that we use the \textit{cut()} function as the criterion function in order to improve the efficiency. Another difference is that we consider floating point values (i.e., structural proximities) between entities instead of binary values.

As the criterion function, \textit{cut()} is designed to calculate both the cohesiveness and the coupling, which measures the distance of two clusters by considering the aggregate inter-connectivity of them. Let \(g_i, g_j\) be two clusters and \(W\) be the structural proximity matrix between entities, the \textit{cut()} between \(g_i\) and \(g_j\) is defined as follows:

\[
\text{cut}(g_i, g_j) = \frac{\sum_{d_i \in g_i} \sum_{d_j \in g_j} W(d_i, d_j)}{|g_i| \cdot |g_j|},
\]

when \(g_i\) and \(g_j\) are the same, it computes the cohesiveness of the cluster, i.e., \(\text{cohesive}(g_i) = \text{cut}(g_i, g_i)\); when \(g_i\) and \(g_j\) are different, it computes the coupling between them, i.e., \(\text{coupling}(g_i, g_j) = \text{cut}(g_i, g_j)\).

Similar \textit{cut()} functions are often introduced in spectral clustering \cite{11,32,53} and information retrieval (e.g., cosine similarity \cite{47}). In our experiment, we also evaluate two popular variations \(|g_i| + |g_j|\) and \(\log(|g_i| \cdot |g_j|)\) instead of the

![Fig. 3. An example about computing structural proximities.](image-url)
The denominator in Formula (3). The experimental results show that our choice is better than the other two denominators, because they sometimes make the sizes of clusters heavily imbalanced (i.e., the skewed partitioning). In addition, using a uniform function to calculate both cohesiveness and coupling is also proposed in [51], called silhouette coefficient.

Our partitioning algorithm is illustrated in Fig. 4, which follows the popular framework of agglomerative partitioning [23]. It accepts as input a set of entities to be clustered. Initially, it constructs a cluster for each entity. The cohesiveness of an entity is its depth in the ontology hierarchy (Line 5). As a result, the more specific entities can be selected earlier for merging. During an iteration, it selects the cluster $g_i$ having the maximum cohesiveness (Line 9) and searches for the cluster $g_j$ that has the maximum coupling with $g_i$ (Line 10). After merging $g_i$ and $g_j$ to create a new cluster $g_{ip}$ (Line 16), it updates the cohesiveness of $g_{ip}$ as well as its coupling with other ones (Lines 17–20). If $g_i$ is fully isolated (Line 13), we set its cohesiveness to zero (a trick in implementation), which implies that selecting it to merge further provides no benefit. The algorithm terminates (Line 11) if the maximum number of the entities in any cluster exceeds $\epsilon$ or there is no cluster whose cohesiveness is larger than zero (indicating that it is unnecessary to continue merging, since every cluster is completely separated). In practice, $\epsilon$ is determined based on the memory requirements of the following matchers such as GMO [27].

One may think that it is costly to update the cohesiveness and coupling when a new cluster is created. In fact, it is not necessary to re-sum the structural proximities between the entities in the new cluster. For instance, let $g_p$ be the new cluster merged from $g_s$ and $g_t$, the sum of the structural proximities in $g_p$ can be computed as follows:

\[
\sum_{d_i \in g_p} \sum_{d_j \in g_p} W(d_i, d_j) = \sum_{d_i \in g_s} \sum_{d_j \in g_s} W(d_i, d_j) + \sum_{d_i \in g_t} \sum_{d_j \in g_t} W(d_i, d_j) + \sum_{d_i \in g_s} \sum_{d_j \in g_t} W(d_i, d_j).
\]

Recall Formula (3), the sum of the structural proximities in $g_s$ (or $g_t$) could be generated by multiplying the cohesiveness of $g_s$ (or $g_t$) to $(|g_s| \cdot |g_s|)$ (or $(|g_t| \cdot |g_t|)$). Also, the sum of the structural proximities between $g_s$ and $g_t$ can be got by multiplying the coupling between $g_s$ and $g_t$ to $(|g_s| \cdot |g_t|)$. In the past steps, the cohesiveness and coupling have already been computed. In our algorithm shown in Fig. 4, we use $\delta$ to represent this optimization (Line 17 and Line 19).

Algorithm: partition($D$, $W$, $\epsilon$).

Input: a set of entities $D$, a matrix $W$ indicating the structural proximities between the entities in $D$ and a parameter $\epsilon$ limiting the maximum number of the entities in each cluster ($\epsilon < |D|$).

Output: a set of clusters $G$.

01 for each entity $d_i \in D$ /* Initialization
02 $g_i = \text{create}(d_i)$;
03 $G = G \cup \{g_i\}$;
04 for each cluster $g_i \in G$
05 cohesive($g_i$) = depth($d_i$); /* depth(root) = 1
06 for each cluster $g_j \in G$ satisfying $j \neq i$
07 coupling($g_i, g_j$) = $W(d_i, d_j)$;
08 while(true) /* Partitioning
09 $g_s = \text{arg max}(\text{cohesive}(g_i))$; /* $g_i \in G$
10 $g_t = \text{arg max}(\text{coupling}(g_i, g_t))$; /* $g_j \in G, g_j \neq g_i$
11 if $|g_s| + |g_t| > \epsilon$ or $\text{cohesive}(g_s) == 0$ /* Termination condition
12 return $G$;
13 else if coupling($g_s, g_t$) == 0 /* Isolated cluster
14 cohesive($g_s$) = 0;
15 else /* Merging
16 $g_p = g_s \cup g_t$;
17 cohesive($g_p$) = cohesive($g_s$) + cohesive($g_t$) + coupling($g_s, g_t$);
18 for each cluster $g_r \in G$ satisfying $i \neq p, s, t$
19 coupling($g_s, g_r$) = coupling($g_s, g_r$) + coupling($g_s, g_r$);
20 coupling($g_t, g_r$) = coupling($g_t, g_r$);
21 $G = G \cup \{g_r\} \setminus \{g_s, g_t\}$;

Fig. 4. Partitioning algorithm.
Compared to some other data clustering approaches [23], our algorithm has two strengths: (1) it is efficient in our context of large ontology matching. The time complexity of our algorithm is $O(n^2)$, where $n$ is the number of entities ($n = |D|$). The maximum times of iterations for partitioning is $n$. In each iteration, the most time-consuming step is updating the coupling of $g_p$ with others (Line 18). It takes at most $k$ times, where $k$ is the number of clusters in that iteration ($k \leq n$). Assuming that we do not sort clusters by the cohesiveness (or coupling), thus selecting $g_i$ (or $g_j$) spends no more than $k$ times. Totally, the time complexity is $O(n^2)$. In general, the time complexity of agglomerative partitioning is at least $O(n^2)$ [23], hence our algorithm has already achieved that lower bound. The time complexity of spectral clustering [11,32,53] (a kind of divisive partitioning) is even higher due to the high computational cost of singular value decomposition ($O(n^3)$); and (2) it is a hierarchical algorithm, which can form a dendrogram (a typical type of tree structure) consisting of layers of clusters at different levels of granularity by saving the merging history. Thus, we can flexibly extract clusters with different scale according to running environment. However, partitional clustering approaches such as K-MEANS [38] require to specify the number of clusters in advance, which is difficult to decide in our scenario. Please note that extensive evaluation on clustering algorithms is out of the scope of this paper.

Let us consider Fig. 5. Based on the structural proximities depicted in Fig. 3, by running the partitioning algorithm illustrated in Fig. 4 (Phase 1.2), the seven entities in Fig. 5 are partitioned into three different clusters $g_1, g_2, g_3$. Every cluster is just a set of entities. From the figure, we find that the partitioning result is reasonable: the four entities about publication are grouped into $g_1$, while classes and properties are separated into disjoint clusters.

### 4.3. Constructing blocks

In the previous subsection, all the entities in an ontology are partitioned into a set of disjoint clusters. However, these clusters cannot be directly used for existing ontology matching approaches, because the RDF triples connecting these entities are missing. Hence, we need to recover the triples to the clusters, i.e., constructing blocks from the clusters (Phase 1.3 in Fig. 1).

A very simple approach is by assigning each RDF triple to a cluster in which at least two entities are contained. For instance, let us see the cluster $g_1 = \{\text{Reference, Book, Inproceedings, Monograph}\}$ in Fig. 2, three triples

$t_4$: (Inproceedings, rdfs : subClassOf, Reference).
$t_5$: (Book, rdfs : subClassOf, Reference).
$t_6$: (Monograph, rdfs : subClassOf, Book).

should be assigned to $g_1$. But, we would immediately recognize that an important restriction structure is omitted: a Reference at least has one Author. In fact, this restriction is useful for many ontology matching approaches [16].

Missing this restriction is caused by leaving out blank nodes. As introduced in Section 2, a blank node is a node that has no intrinsic name [35]. Adopting RDF Sentences [64] rather than RDF triples can preserve more semantic information (e.g., the restriction structure) when constructing blocks from the clusters, even the nested list structure. The entities between different blocks are no longer disjoint, which may lead to additional computational cost. Since each RDF triple belongs to one and only one RDF Sentence [60], such duplicate part at most equals to the number of RDF triples (every cluster includes only an entity). However, the number of overlapped entities in practice is small (less than 3% in our experience), because the number of blocks is much less than the number of entities.

Fig. 5. An example about partitioning.
Let us see the example shown in Fig. 6. The block \( b_1 \) in the right part of the figure includes four RDF Sentences \( s_1, s_2, s_3, s_4 \) (encircled by dashed lines). \( s_1 \) is composed of three RDF triples, and its subject is \textit{Reference}. If we break down the context of \_:genid, the RDF triple \( \text{_:genid, owl: minCardinality, 1} \) would never be assigned. Hence, the restriction structure about a \textit{Reference} at least has one \textit{Author} is destroyed. But, by using RDF Sentences, such RDF triple can be well preserved. Fig. 6 also illustrates the process of constructing a block from a cluster (Phase 1.3): \( b_1 \) is the block generated from the cluster \( g_1 \) (in the left part of the figure), since the subjects of \( s_1, s_2, s_3, s_4 \) are all included in \( g_1 \) (recall Definition 4 in Section 2).

To the best of our knowledge, there is no distance-based clustering technique for directly grouping RDF triples (or RDF Sentences), because: (1) the number of RDF triples in an ontology is much larger than the number of entities. For example, \textsc{galeN} has about 60,000 RDF triples, which is six times larger than the number of its entities; and (2) the distance between two RDF triples is difficult to measure, since an RDF triple has not only three nodes but also an order. Computing the distances between RDF Sentences is even harder.

5. Matching blocks

In the previous section, two large ontologies to be matched have been partitioned into two groups of small blocks. A brute force solution for discovering alignments is by directly matching every pair of blocks in the two ontologies. But, it is not necessary to do so, because it is likely that large portions of one or both of them have no matching counterparts [13].

In this section, we will present a heuristic way of finding matched block pairs, i.e., block mappings. Therefore, only block mappings are further inputted to V-Doc [46] and GMO [27] for alignment discovery. More specifically, a light-weight string comparison technique, I-SUB [55], is firstly employed to exploit anchors between two full ontologies (Phase 2.1 in Fig. 1), and then the blocks from the two ontologies are matched based on the distribution of the anchors (Phase 2.2).

5.1. Finding anchors

We refer to the alignments with high similarities as \textit{anchors}. In our approach, anchors are unnecessarily to be numerous or completely correct, so they can be found by some simple and fast approaches. We employ the following steps to gain anchors between large ontologies.

1. Use I-Sub [55] to automatically generate a set of candidate anchors.
2. Manually remove incorrect ones from the candidate anchors (optional).
3. Manually add some omissions to the candidate anchors (optional).

Please note that the tradeoff between the correctness of anchors and the effort of human interaction should be considered. With the help of some visualization tools such as [1,17], the productivity can be significantly improved. However, manually revising anchors for large ontologies is still time-consuming. In this paper, we do not involve any human interaction during anchor generation.

We briefly introduce I-Sub here. Entities in ontologies contain human readable descriptions in their local names, \texttt{rdfs:label}, \texttt{rdfs:comment} and so on. I-Sub improves the traditional edit-distance [37] based string comparison approaches by considering not only the commonalities between the descriptions of entities but also their differences, hence it is more robust to small diverges from the optimal cutoff taking place. Let \( p, q \) be two strings, the similarity between \( p \) and \( q \) is defined as follows:

\[
\text{sim}(p, q) = \frac{\text{comm}(p, q) - \text{diff}(p, q) + \text{winkler}(p, q)}{\text{comm}(p, q) + \text{diff}(p, q) + \text{winkler}(p, q)},
\]

where \( \text{comm}(p, q) \) stands for the commonality between \( p \) and \( q \), \( \text{diff}(p, q) \) for the difference and \( \text{winkler}(p, q) \) for the improvement of the result by using a correction coefficient introduced in [62].

![Fig. 6. An example about constructing a block from a cluster.](image-url)
If the similarity between two descriptions is greater than a pre-defined value \( \mu (\mu \in [0, 1]) \), then I-SUB would consider the two entities containing those two descriptions as a candidate anchor. In [55], it suggests \( \mu \geq 0.75 \).

Although computing anchors between two whole ontologies takes quite a lot of time in our approach (nearly half of the run time), it compensates for the possibility of missing alignments due to only finding alignments within block mappings. (The anchors generated by I-SUB are re-used as a portion of alignments.) According to our experiment, 10–20% alignments are only found by I-SUB, which demonstrates the effectiveness of calculating anchors between two full ontologies. Besides, based on the OAEI 2007 report [15], at least 50% alignments can be directly found by simple string comparison techniques, so it also provides evidence to support the use of I-SUB. In addition, as compared to other matching techniques [16], I-SUB is very efficient and scalable.

5.2. Generating block mappings

Similarities between blocks can be computed based on the distribution of the anchors gained above. The background idea is that the more anchors can be found between two blocks, the more similar the two blocks are.

Let \( B, B' \) be two sets of blocks from two ontologies \( O, O' \) and \( Q \) be a set of anchors found between \( O \) and \( O' \). anchor\( (b, b', Q) \)
returns the number of the anchors in \( Q \) between two blocks \( b \) and \( b' \) (\( b \in B, b' \in B' \)). The similarity between \( b \) and \( b' \) is defined as follows:

\[
\text{sim}(b, b') = \frac{2 \cdot \text{anchor}\(b, b', Q\)}{\sum_{b \in B \text{ anchor}(b, b', Q)} + \sum_{b' \in B' \text{ anchor}(b, b', Q)}.}
\]

By setting a cutoff \( \eta (\eta \in [0, 1]) \), any two blocks whose similarity is greater than \( \eta \) is selected to make up a block mapping. Our experiment shows that \( \eta \) is stable with various values, because the number of correct anchors is considerably larger than the number of wrong ones, i.e., a few wrong anchors cannot influence the overall distribution. Please note that we permit a block to appear in more than one block mappings because of the difference in large ontology modeling. However, we would see that, in our experiment, the number of block mappings is much less than \( |B| \cdot |B'| \), so the computational cost of further alignment discovery would be largely decreased.

Let us see the example in Fig. 2. Some anchors like \( \langle 3, \text{Book.Book}. = .1, 0 \rangle \) and \( \langle 4, \text{hasAuthor}. \text{hasAuthor}. = .1, 0 \rangle \) might be easily discovered, because the entities in each anchor have the same local names. Next, some block mappings like \( \langle 1, b_1, b'_1, 1.0 \rangle \) can be detected.

6. Discovering alignments

Each block in a block mapping is just a small sub-ontology. Now, we can use various existing ontology matching techniques to discover alignments between the blocks in each block mapping. In this paper, we specifically integrate two powerful matchers, V-DOC [46] and GMO [27], to support alignment discovery, because they are representatives of two kinds of popular ontology matching technology, i.e., the linguistic matching and the structural matching. Our previous experiment showed that they perform better than other similar approaches such as [37,41]. However, we should keep in mind that some other methods [16,19] can also be freely chosen as alternatives. Due to the technical details of V-DOC and GMO have been published in [46,27], in this section we only generally summarize their distinguishing features.

6.1. Linguistic matching

V-DOC adopts a linguistic approach to ontology matching, whose novelty lies in the construction of virtual documents. Basically, as a collection of weighted words, the virtual document of an entity in an ontology contains not only the local descriptions (e.g., rdfs:label), but also some neighboring information to reflect the intended meaning of the entity. Document similarities can be calculated by traditional vector space techniques (e.g., TF/IDF [47,57]) and further be used in similarity-based approaches to ontology matching. Technically, the RDF graph structure is exploited to extract the description information from three sorts of neighboring entities, subject neighbors, predicate neighbors and object neighbors, based on their positions in RDF triples.

6.2. Structural matching

GMO is an iterative structural matcher, which uses RDF Bipartite Graphs [24] to represent ontologies (there exist two kinds of vertices in an RDF Bipartite Graph: entity vertices and triple vertices) and computes structural similarities between entities by recursively propagating their similarities in the bipartite graphs. The basic idea is as follows. The similarity of two entities from two ontologies comes from the accumulation of similarities from the involved RDF triples taking the two entities as the same role (subject, predicate or object) in the triples, while the similarity of two triples comes from the accumulation of similarities from the involved entities as the same role in these two triples being compared. GMO takes a set of
external alignments as input, which are typically found beforehand by other matchers (in our current implementation, the external alignments come from V-DOC) and incrementally generates new additional alignments as output. The performance of GMO improves with the accuracy of external alignments increases.

6.3. Similarity combination strategy

Similarity combination is an important and difficult issue in building ontology matching systems. We propose a heuristic strategy to tune the thresholds (or cutoffs) of our matchers gradually based on the measures of linguistic comparability and structural comparability, which makes the combination robust in a variety of ontology matching scenarios.

Our combination strategy follows the two-step method [4,18], which is a sequential composition of matchers [16,54], (Coma [13] and RMOM [58] use parallel compositions.) First, we calculate the linguistic comparability by measuring the proportion of candidate alignments against the minimum number of entities in two ontologies. The intuition is as follows. If the number of alignments is close to the number of entities in the smallest ontology, we are nearly done with matching, and it is unnecessary to execute GMO any more. Then, we determine the threshold of V-DOC based on the linguistic comparability in order to select the strong (i.e., more reliable) alignments.

If the alignments are not enough (e.g., for low overlapped ontologies, the number of alignments might be considerably smaller than the number of entities in the smallest ontology), then we start the second step. The structural comparability is measured by the cosine similarity, which compares which built-in properties are used between two ontologies, and how often. It is used to determine the threshold of GMO to obtain the weak (i.e., less reliable) alignments.

We divide these two kinds of comparability into three levels (i.e., low, medium and high) to automatically determine the similarity combination strategy. For example, if the linguistic comparability is high, our approach would lower the threshold of V-DOC, then more alignments from V-DOC can be combined to the final alignments. For another example, if the linguistic comparability and the structural comparability are both low, our approach would combine less alignments from V-DOC and GMO to the final result but make the alignments from V-DOC more than the ones from GMO, because the alignments from V-Doc are assumed to be more reliable than the ones from GMO.

We adopt a greedy alignment selection algorithm [25] to select the final alignments. Here, the anchors generated by I-SUB are also considered. More specifically, we choose alignments with multiple iterations. In an iteration, the candidate alignment with the highest similarity is selected, and all its conflicting alignments are removed. (We only permit each entity to appear in one alignment. Therefore, if an alignment that contains the entity d is chosen, then all the other candidates that include d would be deleted.) The process terminates until no candidate is left.

Please consider the example in Fig. 2 again. Although by using I-SUB, we can find three alignments (i.e., anchors), each one contains the entities having the same names. The alignment between Reference and Entry and the alignment between Inproceedings and ConferencePaper cannot be directly found, because they do not have similar names. However, a human may still recognize that they should be alignments because of the similar contexts of the ontologies. V-DOC can utilize neighboring information, hence, regarding Reference for instance, it imports the names of hasAuthor, Book and Inproceedings. By using the neighboring information, V-DOC detects Reference and Entry should be an alignment. Next, GMO finds that the two ontologies has similar graph structures, hence it propagates similarities in the two graphs. As a result, the alignment between Inproceedings and ConferencePaper can be discovered.

Supposing that V-DOC can also find the three alignments containing the entities with the same names, the number of alignments found by V-DOC is 4, and the minimum number of the entities in O, O' is 5. Hence, the linguistic comparability of O and O’ is 0.8. The two ontologies O, O’ share five built-in properties: rdfs:subClassOf, rdfs:domain, rdfs:range, owl:minCardinality and owl:onProperty. As an example, the number of rdfs:subClassOf in O, O’ is 5 and 3, respectively. The number of the other built-in properties is 1, respectively. The cosine similarity between those built-in properties is 19/√29 : 13 = 0.98, where 19 = 5 · 3 + 1 + 1 + 1 + 1, 29 = 5² + 1 + 1 + 1 + 1, 13 = 3² + 1 + 1 + 1. So, the structural comparability is 0.98. Since both the linguistic comparability and the structural comparability are in the high level, the five alignments are all combined as the final result for output.

7. Evaluation

We have implemented the proposed approach in Java, called PBM Partition-based Block Matching) and integrated it into our ontology matching system FALCON-AO [29], which participated in the last OAEI 2007 campaign [15] and was recognized by the organizers as one of the best matching systems. In this section, we will report the results of an experimental study on synthetic and real world data sets. The test cases and experimental results are all available at our web site. All the tests are carried out on an Intel Core 2 Duo 2.13 GHz desktop machine with 2 GB DDR2 memory under Windows XP Professional operating system (SP2) and Java 1.6 compiler. Some parts of evaluation results regarding the real world data sets are quoted from [15].

7.1. Synthetic test

We will measure the performance of PBM on partitioning ontologies as well as on finding block mappings.

7.1.1. Data sets

In our evaluation, we choose two pairs of ontologies: Russia12 and TourismAB, which can be downloaded from the web site. The reasons for selecting them as the test cases are: (1) they come from real world domains and widely used in the field of ontology matching, (2) their sizes are moderate. If the sizes of ontologies are too small, it is unnecessary to partition them into blocks; while if the sizes are too large, they are not appropriate for human observation; and (3) they have open reference files that contain alignments between entities, which are useful for evaluating block mappings. Short descriptions of the two pairs of ontologies are given below.

- **Russia12.** The two ontologies are created independently by different people from the content of two travel web sites about Russia. Russia1 contains 151 classes and 76 properties. Russia2 contains 162 classes and 81 properties. The reference alignment file contains 85 alignments.
- **TourismAB.** The two ontologies are created separately by different communities describing the tourism domains of Mecklenburg–Vorpommern (a federal state in the northeast of Germany). TourismA contains 340 classes and 97 properties. TourismB contains 474 classes and 100 properties. The reference alignment file contains 226 alignments.

7.1.2. Experimental methodology and evaluation metrics

The ideal block mappings should provide both good partitioning quality and good mapping quality. The partitioning quality reflects the effectiveness of the partitioning algorithm, while the mapping quality indicates the possibility of discovering alignments further. In order to measure these two kinds of quality, three experiments are designed for evaluation.

In the first experiment, three volunteers are trained to set up blocks as gold standards manually for evaluating the partitioning quality. However, constructing reference blocks is not an easy job, everyone has his/her own opinion on partitioning, so the reference blocks built here are only generally agreed by all the volunteers. We assess the partitioning quality by comparing to the reference ones. In the experiment, the number of the reference blocks is as follows: 22 ones for Russia, 22 ones for Russia2, 18 ones for TourismA and 23 ones for TourismB. In order to make the number of the blocks from any ontology constructed by PBM the same as the number of the reference ones, we temporarily change the termination condition of our partitioning algorithm (in the real world test, we strictly obey the termination condition in Fig. 4). Technically, we set $\epsilon$ large enough ($\epsilon = 1000$). During partitioning, once the number of the computed blocks equals to the number of the reference ones (it can be satisfied in the test), the partitioning algorithm stops immediately. This kind of approach is widely adopted in data clustering [23].

We use a well-known metric **entropy** to compare the automatically generated blocks with the manually established references. Before introducing the metric, we firstly describe a basic operation (**prec**), which measures the precision of a computed block with respect to a reference one. Let $B$ be a set of computed blocks ($|B| = n$) and $R$ be a set of manual ones ($|R| = m$). $b_i$ denotes a block in $B$, while $r_j$ denotes a block in $R$. $|b_i|$ returns the number of entities in $b_i$, and $|r_j|$ is defined analogously. $b_i \cap r_j$ calculates the common entities in both $b_i$ and $r_j$. The prec of a computed block $b_i$ referring to $r_j$ is defined as follows:

\[
\text{prec}(b_i, r_j) = \frac{|b_i \cap r_j|}{|b_i|}. \tag{7}
\]

The **entropy** measures the distribution (or disorder) of entities in blocks and reflects the overall partitioning quality. The entropy of each block indicates its precision dispersal over the global partitioning. A smaller score indicates a better partitioning quality. The best possible entropy score is 0, and the worst is 1. The entropy of a set of computed blocks $B$ is defined as follows:

\[
\text{entropy}(B) = \frac{1}{\sum_{i=1}^{n} |b_i|} \sum_{i=1}^{n} \text{entropy}(b_i) \cdot |b_i|, \tag{8}
\]

\[
\text{entropy}(b_i) = -\frac{1}{\log m} \sum_{j=1}^{m} \text{prec}(b_i, r_j) \cdot \log(\text{prec}(b_i, r_j)). \tag{9}
\]

For the criterion function that we propose in the partitioning algorithm (see Formula (3)), there are several possible variations about the denominator. So, we also compare two other popular choices, $|g_i| + |g_j|$ and $\log(|g_i| \cdot |g_j|)$, with our **cut()** function.

In the second experiment, we evaluate the mapping quality of computed block mappings by measuring the correctness with different number of those block mappings. The background idea is as follows. The higher the quality of those block
mappings is, the more potential alignments could be found in such block mappings. Furthermore, the correctness also implies the upper bound if only matching the blocks in block mappings. Let $O, O'$ be two ontologies and BM be a set of computed block mappings ($|\text{BM}| = l$). $bm_k$ denotes a block mapping in BM. $bm_k.b, bm_k.b'$ are two blocks in $bm_k$ from $O, O'$, respectively. Let $A$ be a set of alignments in a reference alignment file ($|A| = n$). $a_i$ denotes an alignment in $A$. $a, d, a', d'$ are two entries in $a_i$ from $O, O'$, respectively. The correctness of BM is defined as follows:

$$\text{correctness}(BM) = \frac{1}{n} \sum_{k=1}^{l} \left| \{a_i | a_i \in A, a_i \cdot d \in bm_k.b, a_i \cdot d' \in bm_k \cdot b' \} \right|.$$  \hspace{1cm} (10)

The correctness is influenced by two parameters: the cutoff $\mu$ of anchors and the cutoff $\eta$ of block mappings. We firstly use reference alignments as anchors to determine the best $\eta$, and then test various $\mu$ to find whether $\text{PBM}$ is stable with a variety of cutoffs for anchors. Intuitively, the correctness of BM increases when the number of the block mappings increases, i.e., when the cutoff of the block mappings decreases. But, the computational cost of alignment discovery increases as well. Furthermore, an optimal parameter setting obtained in one domain is often reusable for other domains [7], so we choose the best $\mu$ and $\eta$ here and apply them to the real world cases further.

We choose two other block matching approaches for the above two tests. The first one is $\text{BMO}$ [28], which uses a completely contrary process as compared to $\text{PBM}$. The second one is based on $\text{COMA}$ [13], which is a level-based method.\footnote{Because $\text{COMA}$ does not grant users to adjust the desired number of blocks, we have to implement the partitioning algorithm by ourselves according to the paper. However, it is still not clear about how it matches blocks, so we cannot compare its mapping quality with our approach.} Please see Section 3 for more details.

In the third experiment, we make a comparison between the alignments from $\text{PBM}$ and the ones directly generated from $\text{FALCON-AO}$ without partitioning. Because the sizes of the ontologies in $\text{Russia2}$ and $\text{TourismAB}$ are normal, we can execute $\text{I-Sub}, \text{V-Doc}$ and $\text{GMO}$ on the whole ontologies. (Currently, it is impossible for us to do this experiment on large ontologies.) This metric serves as the truly cost of partitioning and block matching in $\text{FALCON-AO}$.

Two standard information retrieval metrics ($\text{precision}$ and $\text{recall}$) are applied to measure the alignments. Let $A$ be a set of computed alignments and $A'$ be a set of reference alignments, the precision and recall of $A$ referring to $A'$ are defined as follows:

$$\text{precision}(A, A') = \frac{|A \cap A'|}{|A|}, \quad \text{recall}(A, A') = \frac{|A \cap A'|}{|A'|}.$$  \hspace{1cm} (11)

### 7.1.3. Experimental results

Firstly, the experimental results of the partitioning quality (entropy) of $\text{PBM}$, $\text{BMO}$ and $\text{COMA}$ are shown in Fig. 7. They indicate that $\text{PBM}$ is dominant in all the four test cases (i.e., the blocks constructed by $\text{PBM}$ are most consistent to human understanding), and $\text{BMO}$ performs better than $\text{COMA}$.

The entropy of $\text{PBM}$ and two other variations to the denominator in Formula (3) is shown in Fig. 8. It indicates that our criterion function is slightly better than the other two denominators. Actually, we find that, although the other two functions may perform well on fully-separated clusters, in case of outliers or clusters including lots of entities that are neighbors, a large cluster tends to swallow all the other clusters and thus, the entities from all the other clusters would be merged into the large one. This is because a larger cluster typically might have a larger number of cross links with other clusters.

Secondly, we evaluate the mapping quality (correctness) of $\text{PBM}$ as compared to $\text{BMO}$. Before making a comparison, we need to determine two key parameters: the cutoff $\mu$ of anchors and the cutoff $\eta$ of block mappings. By using the reference alignments as anchors, with the variation of $\eta$, the correctness of $\text{PBM}$ is shown in Fig. 9, and the number of block mappings is shown in Fig. 10. They indicate that, in the two test cases, when $\eta$ increases, the correctness of the block mappings decreases, and the number of block mappings decreases as well. We can also see that, in most values of $\eta$, the correctness is fine. For instance, in $\text{TourismAB}$, when $\eta = 0.225$, the correctness is still larger than 0.70. It demonstrates that the correctness does
not decrease drastically as \( g \) increases. In the following experiments, we choose \( g = 0.075 \) as the cutoff of block mappings, because the correctness is fairly large, while the number of block mappings is fairly small.

Then, we test a number of \( \mu \) to see whether PBM is sensitive to various cutoffs of anchors. With the variation of \( \mu \) and \( \eta = 0.05, 0.075, 0.1 \), the correctness of PBM is shown in Fig. 11, and the number of block mappings is depicted in Fig. 12. We can observe that, with \( \mu \) increases, i.e., the number of anchors decreases, the correctness of the block mappings keeps high. It implies that PBM is stable with a pretty good accuracy. In the following experiments, we set \( \mu = 0.85 \) as the cutoff of anchors, because a higher cutoff usually yields to more accurate alignments. Besides, Fig. 11 and Fig. 12 also convince that PBM is robust with slight changes on \( g \) (e.g., \( g = 0.05, 0.1 \)).

By adopting \( \mu = 0.85, \eta = 0.075 \), we compare the correctness of PBM with that of BMO. The comparison results are exhibited in Fig. 13. It shows that the mapping quality of the two approaches is good, and BMO is a little better than PBM. Even though
the two parameters are not the best ones (e.g., $\mu = 0.8, 0.9$ and $\eta = 0.05, 0.1$), the correctness of PBM is still comparable (see Fig. 11).

More specifically, PBM exploits 39 block mappings for Russia12 and 33 ones for TourismAB, while BMO constructs 25 block mappings for Russia12 and 26 ones for TourismAB. Therefore, the potential computational cost of PBM on discovering alignments is higher than that of BMO. However, the number of block mappings is still much smaller than the product of the number of two sets of blocks (22 $\times$ 22 = 484 for Russia12 and 18 $\times$ 23 = 414 for TourismAB). It demonstrates that each block only corresponds to a small number of other ones. Besides, Fig. 13 also implies that, if we only find alignments within block mappings, 15% alignments for Russia12 and 9% ones for TourismAB would never be found by PBM.

If we go further to observe the run time spent by PBM and BMO during partitioning ontologies and matching blocks, we would immediately find that PBM is more efficient than BMO. Based on the current implementation, PBM takes only 5 seconds and 8 seconds to complete the Russia12 and TourismAB cases respectively (including the parsing time), while BMO spends nearly 15.5 min and 30 min. More importantly, BMO would suffer from the scalability problem, because it matches two full ontologies firstly. Therefore, BMO is not feasible for large ontologies.

Thirdly, we directly apply FALCON-AO without partitioning to the whole ontologies in Russia12 and TourismAB and compare the results with the alignments found by PBM. The experimental results are depicted in Fig. 14. Basically, some alignments would be lost because of partitioning. For example, in Russia12, FALCON-AO without partitioning outperforms 6% in recall, which means that 6% alignments are not found by PBM. But, in TourismAB, we interestingly find that PBM discovers more alignments than FALCON-AO without partitioning does. The reason for this situation is that more alignments found by GMO are combined into the final alignments, since the structures of blocks tend to be more similar after partitioning. But, GMO also involves some wrong alignments, thus the precision of PBM is always worse than that of FALCON-AO without partitioning. However, the experimental results demonstrate that PBM does not lose too much precision or recall.
Based on the experimental results above, we conclude that PBM is efficient to achieve both good partitioning quality and good mapping quality.

7.2. Real world test

We will report the results of PBM on discovering alignments in two large real world ontology matching tasks: Anatomy and Food. It is also worthy of noting that our approach has been used and tested in several real-life applications, such as book integration [61] and query rewriting for art thesauri [26].

7.2.1. Data sets

In OAEI 2007, the organizers provided three large ontology matching tracks: Anatomy, Food and Library. All of them are blind tests, i.e., participants do not know the references beforehand, and organizers help evaluate the results. Since the ontologies in the Library task are written in Dutch, most ontology matching tools cannot handle this language and do not present any results on this test, we ignore it here. Short descriptions of the Anatomy and Food tasks are given below.

- **Anatomy.** The ontologies of the Anatomy track are the NCI Thesaurus describing the human anatomy (denoted by Human), published by the National Cancer Institute (NCI), and the Adult Mouse Anatomical Dictionary (denoted by Mouse), which is developed as part of the Mouse Gene Expression Database project. Human contains 3304 entities, while Mouse contains 2743 entities. The two ontologies are represented as complex graphs.

- **Food.** The test case is a taxonomy task in which the hierarchies come from thesauri, and it has a lot of multi-lingual texts. It includes two ontologies: AGROVOC, which is developed by Agriculture Organization (FAO), and NALT, which is developed by United Nations Food Organization. AGROVOC contains 28,439 entities, while NALT contains 42,326 entities. The two ontologies are represented as simple tree structures.

7.2.2. Experimental methodology and evaluation metrics

We compare the alignments generated by PBM to the ones found by the other three ontology matching tools, DSSIM [43], RiMOM [58] and Prior+ [39], which also participated in OAEI 2007. Besides, COMA [13] attended the Food task in OAEI 2006, which is exactly the same as the one in OAEI 2007, and AOAS [63] is a domain-specific tool, which typically aims at matching life-science ontologies and achieved the best performance in the Anatomy track in OAEI 2007. Hence, we also compare COMA and AOAS with PBM. For more details, please see Section 3.

In OAEI 2007, the organizers also provided several matching tasks with small ontologies, such as Benchmarks and Directory, and many ontology matching tools participated in these tracks. Although our tool, FALCON-AO, is one of the best matching tools, there exist several tools that performed slightly better than ours in these tracks. For instance, OLA2 [33] and Prior+ outperformed FALCON-AO in the Directory track, which involves about 4500 cases, each containing two small ontologies. Because we focus on making a comparison on matching large ontologies rather than matching a large amount of ontologies, we do not present the results of these tracks in this paper. For more details, we refer the reader to the OAEI 2007 report [15].

The performance of PBM, DSSIM, RiMOM, Prior+, COMA and AOAS are measured based on precision and recall. Also, the execution time is evaluated.

In this experiment, the parameters of PBM are configured as follows: (1) \( \varepsilon = 500 \), i.e., the number of entities in any block is less than 500. This value is set based on the memory requirements of V-DOC and GMO; and (2) \( \mu = 0.85 \) and \( \eta = 0.075 \), which are gained from the synthetic test.

![Fig. 15. Precision and recall of PBM, DSSIM, RiMOM, Prior+, COMA and AOAS: (a) precision, and (b) recall.](http://oaei.ontologymatching.org/2007/)
7.2.3. Experimental results

The comparison results of the precision and recall of PBM, DSSIM, RIMOM, PRIOR+, COMA and AOAS are illustrated in Fig. 15. The figure indicates that AOAS performs best in the Anatomy track as compared to the other five tools, which demonstrates the effectiveness of using domain knowledge in ontology matching. In fact, AOAS is the best tool in the Anatomy track in OAEI 2007. PBM outperforms the other four generic tools, DSSIM, RIMOM, PRIOR+ and COMA, in average precision and recall and is only slightly behind AOAS, which means that our divide-and-conquer approach can solve the large ontology matching problem. It also proves that, even without using domain knowledge, PBM can generate accurate alignments and guarantee a good coverage.

The execution time of PBM, DSSIM, RIMOM, PRIOR+ and AOAS is shown in Table 1. (COMA does not provide its complete execution time yet.) It shows that PBM is the most efficient one. Please note that, in the Food track, RIMOM and PRIOR+ do not execute all the matching strategies, but only use the edit-distance based strategies as alternatives, and the run time of PRIOR+ excludes the preprocessing stage. DSSIM manually partitions the ontologies into several small pieces. Besides, it also shows that, because of using domain knowledge, AOAS takes more time to achieve better precision and recall.

Based upon the experimental results, we conclude that PBM achieves good precision and recall with significant reduction of run time.

It is also interesting to analyze the portions of the alignments found by each matcher (i.e., I-SUB, V-DOC and GMO) within the final alignments. We collect the alignments generated by each matcher and examine how many alignments are discovered by exactly one, two or three matchers as compared to the final alignments. The analysis is illustrated in Fig. 16. It shows that every matcher contributes quite a large number of alignments to the final results, so it proves that each matcher takes effect in matching large ontologies. Many alignments are combined from more than one matchers, so the accuracy is well guaranteed. Besides, we could also observe that more alignments come from I-SUB and V-DOC than GMO, which demonstrates that matching large ontologies from the linguistic perspective is more reliable than matching from the structural perspective, because large ontologies tend to contain well annotated linguistic descriptions. Furthermore, the portion of the alignments discovered by V-DOC and GMO reflects the additional computation due to the overlapping between blocks, while the portion of the alignments only generated by I-SUB indicates the number of alignments PBM would omit if we only find alignments within block mappings, so using I-SUB to generate anchors over two full ontologies compensates for the possibility of missing alignments due to block matching.

8. Conclusion

In summary, the main contributions of this paper are listed as follows:

- We have introduced a divide-and-conquer approach to matching large ontologies. Not only does it solve the scalability problem, but it also achieves good precision and recall with significant reduction of execution time.

<table>
<thead>
<tr>
<th>Table 1</th>
<th>Execution time of PBM, DSSIM, RIMOM, PRIOR+ and AOAS</th>
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<tbody>
<tr>
<td>Anatomy</td>
<td>PBM: 12 min</td>
</tr>
<tr>
<td>Food</td>
<td>PBM: 6 h</td>
</tr>
</tbody>
</table>

Fig. 16. Percentages of the alignments found by I-SUB, V-DOC and GMO.
We have designed a structure-oriented partitioning algorithm to partition the entities of each RDFS or OWL ontology into a set of small clusters and use RDF Sentences as basic units to construct blocks from the clusters. It both controls the sizes of blocks and guarantees the completeness of blank nodes. Furthermore, it is practical for current ontology matching technology.

We have proposed a heuristic strategy to block matching in terms of the distribution of anchors, which avoids matching each pair of blocks. Furthermore, the anchors can be combined into the final alignments as an important compensation for block matching.

We have integrated two powerful matchers, V-DOC and GMO, to discover alignments in each block mapping. These two matchers discover alignments from different perspectives, and our combination strategy is flexible.

We have implemented our prototype in Java and experimentally evaluated our approach on both synthetic and real world data sets. In the synthetic test, we define the partitioning quality and the mapping quality to measure our approach on partitioning ontologies and finding block mappings. In the real world test, the results from OAEI 2007 demonstrate that our approach can achieve good precision and recall in short time.

In the future work, we look forward to implementing a public Web interface to make the technology widely accessible and effectively interacted with users. We hope to consider certain random picking or sorting techniques to improve our approach further, especially to decrease the run time of finding anchors. We also want to apply some ontology summarization approaches to blocks so that block mappings can be discovered quickly only based on the summaries. Finally, we would like to go beyond matching large ontologies and cope with large database schemas and XML schemas in order to support data integration between different data models.

Acknowledgements

This work is funded in part by the NSFC under Grant 60573083 and also in part by the 973 Program of China under Grant 2003CB317004. We appreciate Christian Mellicke and Willem van Hage for providing the Anatomy and Food data sets, respectively. We also thank Miklos Nagy, Jie Tang and Ming Mao for useful discussion on DSSIM, RIMOM and PRIOR+, respectively. Finally, we are very grateful to Christophe Guéret, Zhisheng Huang, Shenghui Wang and anonymous reviewers for their valuable comments.

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